FMPC 10 % show making affects - Updated June 20:

HW Mark: 10 9 8 7 6 RE-Submit

Real Numbers & Radicals

226



This booklet belongs to: Manson Louis

Period 4

LESSON #	DATE	QUESTIONS FROM NOTES	Questions that I find difficult
1	sept-25/14	Pg. 5 - 8	18
2	Sept 29/14	Pg. 7-11	49,50
3	OCT, 1/19	Pg. 12-17	71,73,100
닉	oct.2/14	Pg. 18 - 23 × 152	141, 142, 156.
5	Oct. 6/14	Pg. 24-30	#185, #194, #1
6	Oct. 8/14	Pg. 31-37	#227,#228,#232,
	Oct.9/14	Pg. QUIZ	2
		Pg.	
		Pg.	
	÷t.	Pg.	
		REVIEW	
	Ŭ	october 16/14TEST	

Your teacher has important instructions for you to write down below.

V=page checked, corrected, and marked

The Real Number System

STRAND		DAILY TOPIC	EXAMPLE
Algebra & Number		Minorthe (12) Che during the Carlo	
B1.	1,1	Determine the prime factors of a whole number,	
Demonstrate an understanding of factors	1.2	Explain why the numbers 0 and 1 have no prime factors.	,
of whole numbers by determining the:	1.3	Determine, using a variety of strategies, the greatest common factor or least common multiple of a set of whole numbers, and explain the process	
 Prime factors Greatest Common Factor Least Common 	1.4	Determine, concretely, whether a given whole number is a perfect square, a perfect cube or neither.	
Multiple • Square root • Cube root	1.5	Determine, using a variety of strategies, the square root of a perfect square, and explain the process.	
	1.6	Determine, using a variety of strategies, the cube root of a perfect cube, and explain the process.	
	1.7	Solve problems that involve prime factors, greatest common factors, least common multiples, square roots or cube roots.	
B2.	2,1	Sort a set of numbers into rational and irrational numbers.	
Demonstrate an understanding of	2.2	Determine an approximate value of a given irrational number.	
irrational numbers by:Representing,	2.3	Approximate the locations of irrational numbers on a number line, using a variety of strategies, and explain the reasoning.	
identifying and simplifying irrational	2.4	Order a set of irrational numbers on a number line.	
numbers. • Ordering irrational	2,5	Express a radical as a mixed radical in simplest form (limited to numerical radicands).	
numbers	2.6	Express a mixed radical as an entire radical (limited to numerical radicands).	
	2.7	Explain, using examples, the meaning of the index of a radical.	
	2.8	Represent, using a graphic organizer, the relationship among the subsets of the real numbers (natural, whole, integer, rational, irrational).	
		as ICNI Connections IRI Personing [ME] Mental Mathematics	

[C] Communication [PS] Problem Solving, [CN] Connections [R] Reasoning, [ME] Mental Mathematics [T] Technology, and Estimation,

[V] Visualization

Vare	Terms
Kev	Terms

Key Terms			
Term	Definition	Example	
Real Number (R)	All numbers that can be placed on a number line	$1, 2.\overline{5}, \sqrt{2}$	
Rational Number (Q)	Numbers that can be written	5, 2.13, ½	
Irrational Number $(ar Q)$	# cannot be written as fraction,	$\sqrt{2}$, π , $\sqrt{3}$	
Integer (Z)	All positive inegative #5	-2,-1,0,1,2	
Whole Number (W)	and zero. All positive numbers and zero	0,1,2,3	
Natural Number (N)	(no decimal) All positive numbersabut NOT	1,2,3	
Factor	Numbers vou can multiply tog. to get and A method to obtain the prime	mer # a factor of 6 = 2	
Factor Tree	factors of a number using a	2 4 = 2 × 2 2 2 4 = 2 z	
Prime Number	tree snaperform. A # only divisible by 2 and 11501f.	27,3,11	
Prime Factorization	The act of writing a number (or an expression) as a product of PRIME #s	24 3 × 23 × 23 × 23 ×	
GCF .	"Greatest common factor" = the largest # that divides evenly into 2 or more #5	GCF OF 20 and 16:4	
Multiple	the result of multiplying a # by	First 3 multiples of 8: 8,16,24	
LCM	"Least Common Multiple" the smallest multiple shared between 2 or more #	6 (0.00)	
Radical	Name given to square roots, cube	√36, ³ √49	
Index	Represents what root the radical	index X	
Root Square root Cube root	Finding theroot savare 1901, cube 1001s means what number will multip itself 2 or 3 times to getlement the	1 C-11 - 0 10 - 1 - 1 - 1 - 0 17	
Power	designated# I an expression made up of an exponent & base	base 34-exponent & power	
Entire Radical	a radical where all nunverter are underneath the radical sign	√ 5	
Mixed Radical	A radical with an integer outside of the radical sigh (left).	2√15	
	/	93	

A Tells you what

A number made up of a rational number and an irrational #.

mind of root

The Real Number System

Real numbers are the set of numbers that we can place on the number line.

Real numbers may be positive, negative, decimals that repeat, decimals that stop, decimals that don't repeat or stop, fractions, square roots, cube roots, other roots. Most numbers you encounter in high school math will be real numbers.

The square root of a negative number is an example of a number that does not belong to the Real Numbers.

There are 5 subsets we will consider.

Real Numbers

Rational Numbers (Q)

Numbers that can be written in the form $\frac{m}{n}$ where m and n are both integers and n is not 0.

Rational numbers will be terminating or repeating decimals.

Eg. 5, -2. 3,
$$\frac{4}{3}$$
, $2\frac{3}{8}$

Natural (N)	Whole (W)	<u>Integers</u> (Z)
{1, 2, 3,}	{0, 1, 2, 3,}	{,-3,-2,-1, 0, 1, 2, 3,}

Irrational Numbers (\bar{Q})

Cannot be written as $\frac{m}{n}$.

Decimals will not repeat, will not terminate.

Eg. $\sqrt{3}$, $\sqrt{7}$, π , 53.123423656787659...

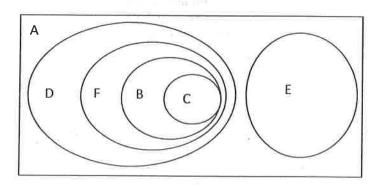
Name all of the sets to which each of the following belong?

Name an of the sets to which each	in of the following belong?	
1. 8	2. 4/5	3. $\frac{15}{5}$ = 3
Q, Z, W, N	Q	Q , Z, W, N
4. √ 7	5. √0.5 O	6. 12.34
Q	, , ,	Q
7. —17	8. $-\left(\frac{2}{3}\right)^3 = -\frac{8}{27}$	9. 2.7328769564923
Q,Z	27	Q

Write each of the following Real Numbers in decimal form. Round to the nearest thousandth if necessary. Label each as Rational or Irrational.

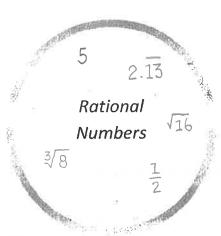
10. $\frac{2}{9}$ Q		$-3\frac{3}{7}$ Q	12. √8 Q
0.222		-3.429	2.828
13. ³ √9 Q		14. ∜ 256 Q	15. ∜25 Q
2.080	A	4	1.904

16. Fill in the following diagram illustrating the relationship among the subsets of the real number system. (Use descriptions on previous page)

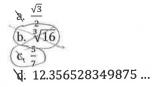


- A Real Numbers
- B Whole Numbers
- c Natural Numbers
- p Rational Numbers
- E Irrahanal Numbers
- Fintegers

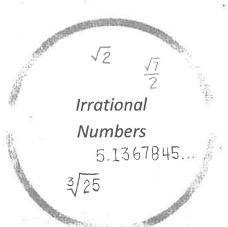
- 17. Place the following numbers into the appropriate set, rational or irrational.
 - 5, $\sqrt{2}$, $2.\overline{13}$, $\sqrt{16}$, $\frac{1}{2}$, $5.1367845 \dots$, $\frac{\sqrt{7}}{2}$, $\sqrt[3]{8}$, $\sqrt[3]{25}$



★ 18. Which of the following is a rational number?



- 20. To what sets of numbers does -4 belong?
 - a, natural and whole
 b. irrational and real
 c, integer and whole
 d. rational and integer



19. Which of the following is an irrational number?

- 21. To what sets of numbers does $-\frac{4}{3}$ belong?
 - a. natural and whole b. irrational and real c. integer and whole
 - d. rational and real

Your notes here	Your	notes	here
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Page 6 | Real Numbers Key



The Real Number Line



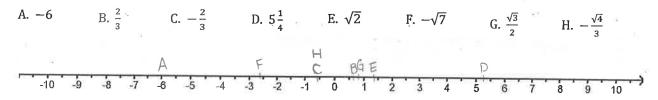
All real numbers can be placed on the number line. We could never list them all, but they all have a place.

Estimation:

It is important to be able to estimate the value of an irrational number. It is one tool that allows us to check the validity of our answers.

Without using a calculator, estimate the value of each of the following irrational numbers.

Show your steps!				
22. $\sqrt{7}$	23. $\sqrt{14}$	24. √75		
Find the perfect squares on either side of 7.	square 1001-3=9	square root 8 = 64		
\rightarrow 4 and 9	square root 4:16	square root 9:81		
Square root $4 = 2$	3000164001710			
Square root 9 = 3	√14 ≈ 3.7	√75 ≈ 8.7		
Guess & Check: 2.6 x 2.6 =6.76	3.7×3.7: 13.69	8.6×8.6=73.96		
$2.7 \times 2.7 = 7.29$		8.7 × 8.7= 75.69		
$\therefore \sqrt{7}$ is about 2.6		71, 7 == 7		
25. ³ √11	26. ³ √90	27. ³ √150		
cube root 2 = 8	Cube root 64:4	Cube 100+ 125:5		
cube root 3 = 27	Cube root 1250			
₹11 ≈ 2.2 22×22×22:10-6	4.5×4.5×4.5 4.5×4.5×4.5	$3\sqrt{150} \approx 5.3$ the number line below.		
28. Place the corresponding le	tter of the following Real Numbers on	the number line below.		



Factors, Factoring, and the Greatest Common Factor

We often need to find factors and multiples of integers and whole numbers to perform other operations.

For example, we will need to find common multiples to add or subtract fractions. For example, we will need to find common factors to reduce fractions.

Factor: (NOUN)

Factors of 20 are {1,2,4,5,10,20} because 20 can be evenly divided by each of these numbers.

Factors of 36 are {1,2,3,4,6,9,12,18,36}

Factors of 198 are { 1,2,3,6,9,11,18,22,33,66,99,198}

Use division to find factors of a number. Guess and check is a valuable strategy for numbers you are unsure of.

To Factor: (VERB) The act of writing a number (or an expression) as a product.

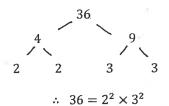
To factor the number 20 we could write 2×10 or 4×5 or 1×20 or $2 \times 2 \times 5$ or $2^2 \times 5$. When asked to factor a number it is most commonly accepted to write as a product of prime factors.

<u>Use powers</u> where appropriate.

Eg.
$$20 = 2^2 \times 5$$

Eg.
$$36 = 2^2 \times 3^2$$
 Eg. $198 = 2 \times 3^2 \times 11$

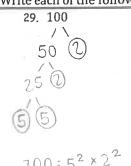
A factor tree can help you "factor" a number.

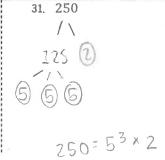


Prime:

When a number is only divisible by 1 and itself, it is considered a prime number.

Write each of the following numbers as a product of their prime factors.





Write each of the following numbers as a product of their prime factors.

wifite each of the following number	ers as a product of their prime facto	rs.	
32. 324	33. 1200	34. 800	
/ \	/\	/\	
162 (2)	400 ③	400 (2)	
/ \	/ \	1	
81 0	200 ②	200 0	
11	100 2	^^	
27 5	100	100 4	Ti.
1\ 324:34 x 2 ²	50(2)	5060	
3) 9		50 0	800:52 x 25
	25 (2)	250	800-5-7-2
(3) (3)		20	
-	(35) 1200 = 5 ² × 3	x 242	10
Greatest Common Factor	. 00 1000	- V	

At times it is important to find the largest number that divides evenly into two or more numbers...the **Greatest Common Factor (GCF)**.

		20	36-3 12
Challenge:	36	148	198=11×32×2
35. Find the GCF of 36 and 198.	2 - 10 2 18	(2) 99	
GCF: 18 36:	2:18	100	2 0 [0]
	:2:18	9 49	3 cx 2 = 18
	(3)(3)	(3)(3)	

Challenge: 36. Find the GCF of 80, 96 and 160.	80 = 5 × 24	96 = 3×25	160=5×25
80 - 40, 20,16	GCF = 16 8 10 4 0 6 6	Q 24 Q 24	9 20 4 10 2
24:16	00	(a) (a)	<u> </u>

DOING HOLES	

Find the GCF of each set of numbers.

rind the GCF of each set of numbers.			
37. 36, 198	38. 98, 28	39. 80, 96, 160	,i. i
$36 = 2^2 \times 3^2$		$80 = 2^4 \times 5$	
$198 = 2 \times 3^2 \times 11$	98 28	$96 = 2^5 \times 3$	
		$160 = 2^5 \times 5$	
Prime factors in common	249 214		
•	6 49 6 1	Príme factors in common	
are 2 and 3^2 .	00 00	are 24.	
GCF is 2 x 3 ² = 18	98:72×2		
4CF 15 2 X 3 = 18		GCF is 24=16	
	28 = 1 × Z²		
	7 ×2=14	(Alternate method:	a a
(Alternate method:		List all factorschoose	
Líst all factorschoose	GCF=14	1	
largest in both lists.)		largest in both lists.)	
the object of th			
40. 24, 108	41. 126, 189, 735, 1470	42. 504, 1050, 1386	2 = 0
$108 = 3^3 \times 2^2$	126:7×32×2 189:7×3	42. 504,1050,1386 504=7×3 ² ×2 ³ 1050=7 ³	x5 - x 3 × 2
100 - 3	101-1/3		
54 24 = 3×23	(1) 63	2 252 105 10	
54 24 - 24		126 (2) (5) 21 (3) (5)	
/ \	(7) 9	1666	
120	33	0 63	
2	735=72×5×3	1386 = 77 × 7 × 32 ×	2
20	1970 = 72	x5x3x2	(
(3)	149 42	(3) (3) 462	
46	0000 0 735	7:	x 3 x 2=
GCF=3×2	2 = 112 \\ \(\mathbb{G} \) 147	231 4	2
GUT-J	7 × 3 = 21 34	9 27	
Multiples and Least Comi	mon Multiple GCF-21	G G	CF=42
		(7)(14)	

Challenge

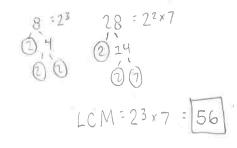
43. Find the first seven multiples of 8.

Challenge

44. Find the least common multiple of 8 and 28.

28, 56

LCM = 56



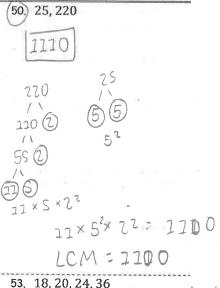
Multiples of a number

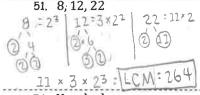
Multiples of a number are found by multiplying that number by {1,2,3,4,5,...}.

Find the first five multiples of each of the following numbers.

	2000 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
45. 8	46. 28	47. 12
8,16,24,32,40,43	28, 56, 84, 112, 140	12,24,36,48,60

Find the least common multiple of e	ach of the following sets of numbers.	
48. 8,28	(49,) 72,90	(50.)
$8 = 2^3$ $28 = 2^2 \times 7$ Look for largest power of each prime factor	72 $3^2 \times 2^3$ 36 ① $90 = 5 \times 3^2 \times 2$ ① 18 30 ③	2:
In this case, 23 and 7. LCM = 23 x 7 LCM = 56	35 50 32 × 23 × 5. = 360 1 LCM = 360	55 /\ (1) (2) (1)
51. 8; 12, 22 8 = 2 ³ 12=3×2 ² 22:11×2	52. 4, 15, 25 4 = 2 ² 15 = 5 × 3 25 = 5 ²	53. 18 : 3 ²





54. Use the least common multiple of 2, 6, and 8 to add:

$$\frac{3}{8} + \frac{5}{6} + \frac{1}{2}$$

$$\frac{9}{24} + \frac{20}{24} + \frac{12}{24}$$
 $\star = \frac{41}{24} \text{ or } 1\frac{17}{24}$

- - 55. Use the least common multiple of 2, 5, and 7 to evaluate:

$$\frac{3}{5} - \frac{2}{7} + \frac{3}{2}$$

$$\frac{47}{70} - \frac{20}{70} + \frac{103}{70}$$

- - 56. Use the least common multiple of 3, 8, and 9 to evaluate:

valuate:
$$\frac{7}{9} = \frac{1}{3} = \frac{1}{8}$$

$$3:3$$
 $9:3^2:2^3 \times 3^2$
 $8:2^3$
 72

$$\frac{50}{72} - \frac{24}{72} - \frac{9}{72}$$

Radicals:

Radicals are the name given to square roots, cube roots, quartic roots, etc.

$$\sqrt[n]{\chi}$$

The parts of a radical:

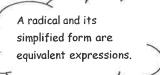
Radical sign Index $\sqrt{}$

(Operations under the radical are evaluated as if inside brackets.) (tells us what type of root we are looking for, if blank...index is 2)

Radicand

n

(the number to be "rooted")



Square Roots

Square root of 81 looks like $\sqrt{81}$. It means to find what value must be multiplied by itself twice to obtain the number we began with.

$$\sqrt{81}$$
 we think ... $81 = 9 \times 9 \rightarrow \sqrt{81} = 9$

$$\sqrt{a^4}$$
 we think ... $a^4 = a^2 \times a^2 \rightarrow \sqrt{a^4} \stackrel{\text{O}}{=} a^2$

PERFECT SQUARE NUMBER: A number that can be written as a product of two equal factors.

 $81 = 9 \times 9$ } 81 is a perfect square. Its square root is 9.

First 15 Perfect Square Numbers:

1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225, ...

Your notes here...

Operations inside a √ must be considered as if they were inside brackets...do them

Evaluate the following.

57.	$\sqrt{49}$

7

0

0

V(25 x -1) = N25 x N-1

59.
$$-\sqrt{36}$$

-6

60. Finish the statement:

I know that $\sqrt{16} = 4$ because...

4×4=16

 $6 \times \sqrt{-1} = 5 i$ 61. Finish the statement:

I know that $\sqrt{\frac{64}{81}} = \frac{8}{9}$ because...

$$\sqrt{8}$$
 8×8=64 $\sqrt{81}$ 9×9=81

62. Finish the statement:

I know that $\sqrt{-36} \neq -6$ because... $-6 \times -6 = +36$

11

64.
$$\sqrt{45-20}$$

$$\sqrt{25} = 5$$

65. $2\sqrt{40-(-9)}$

66. Simplify.
$$\sqrt{x^2}$$

X

67. Simplify.
$$\sqrt{4x^2}$$

2)

68. Simplify. $\sqrt{16x^4}$

 $4\chi^2$

Cube Roots:

PERFECT CUBE NUMBER: A number that can be written as a product of three equal factors.

Cube root of 64 looks like $\sqrt[3]{64}$.

The index is 3. So we need to multiply our answer by itself 3 times to obtain 64. $4 \times 4 \times 4 = 64$

First 10 Perfect Cube Numbers: 1, 8, 27, 64, 125, 216, 343, 512, 729, 1000, ... Evaluate or simplify the following. How could a factor tree 70. ³√8 = 2 69. ³√8 be used to help find Explain what the small 3 in this $\sqrt[3]{125}$? problem means. Do a factor tree for It's asking for the 125 and their should be cube root = the 5 x 5 x 5 72. Evaluate √125. - 5 answer will multiply itself 3 times to obtain 8+(2). 74. ³√1000 = 10 75. ³√-8 = -? 78. 3√−216 = −6 77. ³√343 = 7 76. Show how prime factorization can be used to evaluate $\sqrt[3]{27}$. Find the prime factors of 27 and there should be 3 x 3 x 3 79. $\sqrt[3]{27} \times \sqrt{20 \times 5}$ 80. $\sqrt[3]{64} \times \sqrt{45-20}$ 3 × 10 = 30 83. $\sqrt[3]{a^6} = 0$

Other Roots.

85. How does ⁶√729 differ from ³√729? Explain, do not simply evaluate.

86. Evaluate if possible. $\sqrt[4]{16} = 2$

87. Evaluate if possible. $\sqrt[4]{-16}$. = $\sqrt[4]{-1} \times \sqrt[4]{16}$ $\stackrel{?}{\iota} \times 2$ NOT POSSIBLE

equal numbers to equal 729

 $\sqrt[3]{729}$ is looking for a product of 3 equal #5 to equal 729.

- 89. Evaluate if possible. $\sqrt[4]{81}$.
- 90. Evaluate if possible. $\sqrt[6]{64}$.

2

d a

91. Evaluate if possible. $\sqrt[3]{24-16}$.

3/8 = 2

92. Evaluate if possible. $\sqrt[4]{2(32-24)}$.

→ ¥2(8) → 4√16 = 2 93. Evaluate if possible. $\sqrt[3]{4(5-3)}$.

→ 3/4(2) → 3/8 = 2

Using a calculator, evaluate the following to two decimal places.

94. $\sqrt[3]{27} - \sqrt[5]{27}$

3 - 1.93

95. $2\sqrt{10} + \sqrt[4]{64}$

6.32+2.83

- 9.15

96. $\sqrt[5]{-32} - \sqrt[4]{16}$

[-4,00]

97. 19 – ∛18

19-2-62

98. $\frac{\sqrt{12}-\sqrt[3]{7}}{2}$

· 3.46-1.91

→ <u>1.55</u> <u>.</u> 0.78

99. $\frac{\sqrt[3]{9}-\sqrt[3]{27}}{}$

 $\begin{array}{c} \rightarrow 2.08 - 3 \\ \hline -0.92 = -0.31 \end{array}$

Describe the difference between radicals that are rational numbers and those that are irrational numbers.

rational

irrational

V16

113

All radicals that equal arational are perfect squares, cubes, etc. All radicals that equal irrational #5

Updated June 2013

Evaluate of simplify the folio		
101. 125 = 53 (S) 25 (S) (S) (S) (S) (S) (S) (S) (S) (S) (S)	102. $\sqrt{2(15 - (-3))}$ $\sqrt{2(18)}$ $\sqrt{36}$ = 6	103. $\sqrt{\sqrt{16}}$ $\sqrt{4} = 2$
104. √0.16 0.4	105.	106. $3\sqrt{25} - 4\sqrt[3]{8}$ $3(5) - 4(2)$ $15 - 8$ $= 7$
107. $\sqrt{\frac{1}{4}}$ $\sqrt{0.25}:$ $0.5 \Rightarrow \sqrt{\frac{1}{2}} \Rightarrow$	$ \sqrt{\frac{16}{49}} $	109. $\sqrt{\frac{100}{400}}$ $\frac{10}{20} = \frac{1}{2}$
$\frac{2\sqrt{a^4}}{\sqrt{a^4}}$	111. $\sqrt[3]{-x^6}$ $\sqrt[3]{(-1)} \times \sqrt[3]{x^6}$ $-1 \times x^2$ $-x^2$	112. $\sqrt[3]{8x^3}$ $\sqrt[3]{8} \times \sqrt[3]{\chi^3}$ $\sqrt[2]{\chi}$ $\sqrt[2]{\chi}$

Evaluate or simplify the following.

113. $\sqrt{5^2}$ $\sqrt{25} = \sqrt{5}$

(√5)²

114.

115. $-\sqrt{(-5)^2} - \sqrt{25} = -5$

116. $(\sqrt{49} - \sqrt{64})^3$ $(7 - 8)^3$

 $\sqrt{\sqrt{16}}$ $\sqrt{4}$ 120.

118. What would be the side length of a square with an area of 1.44 cm²?

1-1-2 cm

 $\left(\sqrt[4]{16}\right)^3$

(2)3 = 8

√-32

-2

121. ⁸√256

Z

122. Use the prime factors of 324 to determine if 324 is a perfect square. If so, find $\sqrt{324}$.

Answer:

119.

 $324 = 2^2 \times 3^4$ if fully factored

- $\therefore \sqrt{324} = \sqrt{2 \times 2 \times 3^2 \times 3^2}$
- $\therefore \sqrt{324} = \sqrt{(2 \times 3^2) \times (2 \times 3^2)}$
- $\therefore \sqrt{324} = (2 \times 3^2)$
- $\therefore \sqrt{324} = 18$

YES

123. Use the prime factors of 576 to determine if 576 is a perfect square. If so, find $\sqrt{576}$.

 $\sqrt{576} = \sqrt{3^2 \times 26}$ $-\sqrt{576} = \sqrt{(3 \times 2^3)} \times (3 \times 2^3)$ $= \sqrt{576} = (3 \times 2^3)$ $= \sqrt{576} = 24$ YES

5832

124. Use the prime factors of 1728 to determine if it is a perfect cube. If so, find $\sqrt[3]{1728}$.

125. Use the prime factors of 5832 to determine if it is a perfect cube. If so, find $\sqrt[3]{5832}$.

1728 = $3^{3} \times 2^{6}$ 4 432 $\sqrt[3]{1728} : \sqrt[3]{3} \times 2^{6}$ © © 4 108 $\sqrt[3]{1728} : \sqrt[3]{3} \times 2^{2}) \times (3 \times 2^{2}) \times (3 \times 2^{2})$ © © 54 $\sqrt[3]{1728} : \sqrt[3]{2} \times 2^{2} \times (3 \times 2^{2}) \times (3 \times 2^{2})$ © $\sqrt[3]{9} \sqrt[3]{1728} : \sqrt[3]{5832} : \sqrt[3]{5832}$

 $\sqrt{5832} = \sqrt[3]{3^6 \times 2^3}$ $\sqrt{5832} = \sqrt[3]{3^6 \times 2^3}$ $\sqrt{3^2 \times 2} \times (3^2 \times 2) \times (3^2 \times 2) \times (3^2 \times 2)$ $\sqrt{3^2 \times 2} \times (3^2 \times 2) \times (3^2 \times 2) \times (3^2 \times 2)$

₹5832 : 32×2 = ₹5832 : 18 YES

(3)

126. An engineering student developed a formula to represent the maximum load, in tons, that a bridge could hold. The student used 1.7 as an approximation for $\sqrt{3}$ in the formula for his calculations. When the bridge was built and tested in a computer simulation, it collapsed. The student had predicted the bridge would hold almost three times as much.

The formula was: $5000(140 - 80\sqrt{3})$

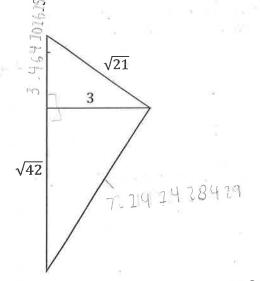
What weight did the student think the bridge would hold?

5000(140-80(17))

= 5000 (140 - 136) = 5000 (4) 20000 tons Calculate the weight the bridge would hold if he used $\sqrt{3}$ in his calculator instead.

7179-676973

130. Calculate the perimeter to the nearest tenth. The two smaller triangles are right triangles.

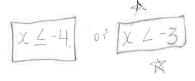


3.464101615+6.480740698 7.142418429 + 47.58 2575

P=21.7 *Units*

127. For what values of x is $\sqrt{x-2}$ not defined?

128 For what values of x is $\sqrt{x+3}$ not defined



129. For what values of x is $\sqrt{5-x}$ not defined

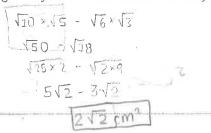


Calculate the area of the shaded region.

 $\sqrt{10}$ cm 7.072067817 $\sqrt{6}$ cm $\sqrt{5}$ cm

131. To the nearest tenth:

 6° S 132. As an *expression* using radicals: (you may need to come back to this one)



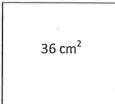
3.46

ble square root is like

finding the Isides lengths of a square (the perfect square the

33. Consider the square below. Why might you 134. Consider the diagram below. Why do you think $\sqrt{}$ is called a square root?

think ³√ is called a cube root?



want to eaval find 2 humbers that multiply together?

bic cube root is like finding 3 side length, of a cube (perfect cube = the volume)



64 cm³

cube root is called cube root b/c the cube has 3 eaval number that

know the requals values 135. Find the side length of the square above.

root o/c it wants to

is-called square



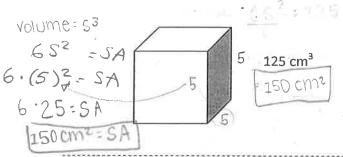
get that answer.

137. Why do you think 81 is called a "perfect square" number? s the area of a Because 81 is the area of a square (9x9 - no decimais)

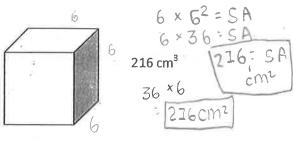
138. Why do you think 729 is called a "perfect cube" number? Because 719 is the volume of a cube (1xwxh) -> cube: all equal side lengths/

widths/ neights (9x9x9)

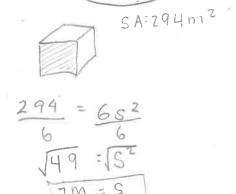
139. Find the surface area of the following cube.



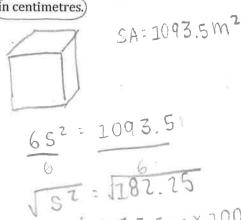
140. Find the surface area of the following cube.



141. A cube has a surface area of 294 m2. Find its edge length in centimetres.



142. A cube has a surface area of 1093.5 m2. Find its edge length in centimetres.)



Multiplying Radicals.

Some notes possibly...

143. Challenge

Evaluate $\sqrt{4} \times \sqrt{9} = \sqrt{36} = 6$

144. Challenge

What single radical has the same value as $\sqrt{4} \times \sqrt{9}$?

What is the product of the radicands?

[36]

145. Challenge

Evaluate $\sqrt{16} \times \sqrt{4} : -\sqrt{64} : \boxed{8}$

146. Challenge

What single radical has the same value as $\sqrt{16} \times \sqrt{4}$?

V64

What is the product of the radicands?

64

147. Based on the examples above, can you write a rule for multiplying radicals?

Multiply values that are infront of the root with values that are in front of the root. Multiply values underneath the root with values underneath the root. *NOTES: Roots must

148. Challenge

Evaluate: $(2)\sqrt{9} \times (5)\sqrt{4}$

(2)(5) × 19(14) = 20 × 136 = 20 × 6 = 60

2 x N9 x 5 x N4

Multiplying Radicals: The Multiplication property

$$\sqrt{a} \times \sqrt{b} = \sqrt{ab}$$
 (this is reversible)

Evaluate Notice...
$$\sqrt{4} \times \sqrt{9}$$
 Rule:
$$2 \times 3 = 6$$

$$= 6$$

$$= \sqrt{36} = 6$$
 Evaluate
$$\sqrt{16} \times \sqrt{4}$$
 Notice...
$$\sqrt{16} \times \sqrt{4}$$

$$\sqrt{16} \times \sqrt{4}$$

$$\sqrt{16} \times \sqrt{4}$$

$$\sqrt{16} \times \sqrt{4}$$

$$\sqrt{16} \times \sqrt{4} = \sqrt{16} \times \sqrt{4} = \sqrt{16} \times \sqrt{4} = 8$$
 Evaluate
$$2\sqrt{9} \times 5\sqrt{4} = 8$$

$$2 \times 3 \times 5 \times 2 = 60$$
 Notice...
$$2\sqrt{9} \times 5\sqrt{4} = 2 \times 5 \times \sqrt{9} \times 4 = 10\sqrt{36} = 60$$

Multiply each of the following. Leave answers in radical form if necessary. We will simplify

1 3				U
radicals	fully	in a	a later	section.

	radicals fully in a later secti	on.	- F
31	$149. \sqrt{6} \times \sqrt{2}$	150. $\sqrt{8} \times \sqrt{2}$	151. $\sqrt{7} \times \sqrt{3}$
	$\sqrt{1}$ 2	VI6 = 197	_
		V 10	$\sqrt{21}$
			9
-	152. $-\sqrt{7} \times \sqrt{7}$	$153.\sqrt{3}\times-\sqrt{3}$	154. $3\sqrt{18} \times -2\sqrt{12}$
	-7.× (√49)	(-1) × √9	-6 × √216
	-L,x (V44)		
	: [7]	= -3	= [-6√216]
	$155\sqrt{5} \times 2\sqrt{20}$	$(156) - 10\sqrt{3} \times \frac{\sqrt{5}}{5} \rightarrow \left(\begin{array}{c} 1 \\ 1 \end{array} \times \frac{\sqrt{5}}{5} \right)$	$(157. \left(\frac{3}{4}\sqrt{2}\right)\left(-\frac{2}{3}\sqrt{3}\right)$
	-2 × √200	$-10 \times \sqrt{3} \times \frac{1}{5} \times \sqrt{5}$	3 × \(\frac{1}{3}\times \sqrt{3}\times \sqrt{3}\times
	-20	10 x \18 = 2 \15	2 X X X X X X X X X X X X X X X X X X X
*:	$158. \left(\frac{3}{4}\sqrt{6}\right) \left(-\frac{2}{3}\sqrt{6}\right)$	$159(\frac{\sqrt{7}}{\sqrt{3}} \times \frac{\sqrt{5}}{\sqrt{2}} \qquad \frac{\sqrt{3} \zeta}{\sqrt{6}}$	$160.\frac{2\sqrt{5}}{\sqrt{3}} \times \frac{5\sqrt{2}}{15\sqrt{7}}$
	3× √6×3×√6	厅/言×厅x壳	
	1 81 - 1	13 13 12	2 × N5 × 5 × NZ
	3 × 3 × 16 × 16	V35 / 1 - V35	√3 × 15 × √7
	-1 \J36 + -1 x1	V35 / 1 - V35	2 10 × VIO 2510
	161. Challenge = -6	p [-3]	3 15×V21 3V22
	Miles FO and a second and a few on a	(-1)	h

Write $\sqrt{50}$ as a product of two radicals as many ways as you can (whole number radicands only).

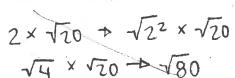
Find the pair from above that includes the largest perfect square and write it here $\rightarrow \sqrt{2} \times \sqrt{25}$

Simplify the perfect square in that pair $\rightarrow \sqrt{2} \times 5 \rightarrow 5\sqrt{2}$

162. Challenge

2 × 14 × 15

Simplify $2\sqrt{20}$ using the previous example. (Think of it as $2 \times \sqrt{20}$.)



2 × 2 × √5 Explain your process...

Find factor Find factors of 20 and find the pair à the biggest perfect square and use that /replace it w the radicand. Then simplify (pefect savarel and put that outside radical sign & multiply wo ther number.

163. What is a mixed radical?

when you have a number outside the root sign and a # inside

164. Challenge

Explain in your words: -Solve 13 x 16 = 128, then you get 2 128 simplify.

Simplify: $2\sqrt{3} \times \sqrt{6}$

2× √3× √6 = 2√18 + 2× √2× √9 = 2× √2×3 + 6√2.

165. Challenge

Challenge Explain in your words: First simplify into 1 mixed radical simplify: $(-3\sqrt{6})(5\sqrt{8}) \quad -3 \times \sqrt{6} \times S \times \sqrt{8} \quad -15 \sqrt{48}$ $-15 \sqrt{48}$ Explain in your words: First simplify into 1 mixed radical radical formula for the first simplify into 1 mixed radical radical formula for the first simplify into 1 mixed radical for the first simplify into 1 mixed radical radical for the first simplify into 1 mixed radical radical for the first simplify into 1 mixed radical radical for the first simplify into 1 mixed radical ra

Your notes here...

Radicals as equivalent expressions:

Eg. 2 and $\frac{6}{3}$ are equivalent expressions. They occupy the same place on the number line. As do $\sqrt{12}$ and $2\sqrt{3}$.

Simplifying radicals gives us a standard way to express numbers. We will follow particular patterns so that each of us writes our answers in the same form. Working in radical form allows us to round answers at the end of our calculations if necessary, creating more accurate solutions.

Simplifying Radicals:

Like fractions, radicals must be simplified to "lowest terms". To do this we must consider what type of radical we are working with.

We will remove part of the number under the radical sign IF an appropriate factor can be found.

To simplify square roots, we look for perfect square factors. We then remove the perfect square from under the radical sign.

Simplify. $\sqrt{50}$

 $\sqrt{50}$ is called an entire radical.

This is not a perfect square, but 50 has a perfect square factor, 25.

 $\sqrt{50} = \sqrt{25 \times 2}$

We know the square root of 25...it is 5. We cannot simplify $\sqrt{2}$.

 $\sqrt{25 \times 2} = 5 \times \sqrt{2}$

We write this as a mixed radical.

 $= 5\sqrt{2}$

Simplify. $2\sqrt{20}$

 $2\sqrt{20} = 2 \times \sqrt{20}$

This reads "2 times the square root of 20."

 $2 \times \sqrt{20} = 2 \times \sqrt{4 \times 5}$

We must now simplify $\sqrt{20}$. 20 has a perfect square factor, 4.

 $2 \times \sqrt{4 \times 5} = 2 \times 2 \times \sqrt{5}$

We write this as a mixed radical.

$$= 4\sqrt{5}$$

Multiply. Answer as a mixed radical.

 $2\sqrt{3} \times \sqrt{6}$

 $2\sqrt{3\times6}$

We can multiply non-radical numbers and we can multiply radicands.

 $= 2\sqrt{18}$

Now simplify the new radical.

 $= 2 \times \sqrt{9 \times 2}$

The radicand, 18, has a perfect square factor, 9.

 $= 2 \times 3 \times \sqrt{2}$

Write as a mixed radical.

 $= 6\sqrt{2}$

Multiply. Answer as a mixed radical.

 $(-3\sqrt{6})(5\sqrt{8})$

 $= (-3 \times 5 \times \sqrt{6} \times \sqrt{8})$

Multiply non-radicals, multiply radicands

 $= -15 \times \sqrt{48}$

 $=-15\sqrt{48}$

 $=-60\sqrt{3}$

 $=-15\times\sqrt{16\times3}$ $=-15\times4\times\sqrt{3}$

Simplify radical

-35 × 48 -15/48

Key process:

Entire radical

vs

Mixed radical

-15 × 13×16

-15 x 4 x 53

Page 24 | Real Numbers Key

-60 V3

Alternative method: Factorization of Radicand

To simplify square roots, we can write the radicand as a product of its primes. We then look for factors that are present twice (square roots) or three times (cube roots). We then remove the perfect square from under the radical sign.

Simplify. $\sqrt{50}$

 $\sqrt{50} = \sqrt{5 \times 5 \times 2}$ radical.

We write this as a mixed radical.

 $=5 \times \sqrt{2}$

 $= 5\sqrt{2}$

Simplify. $3\sqrt{20}$

 $3\sqrt{20} = 3 \times \sqrt{20}$

 $3 \times \sqrt{20} = 3 \times \sqrt{(2 \times 2) \times 5}$

 $3 \times \sqrt{4 \times 5} = 3 \times 2 \times \sqrt{5}$

The factor 2 is present twice, it comes out as 2.

Multiply the two rational numbers in front the radical.

When a factor is present twice, it can be removed (as a single) from under the

 $= 6\sqrt{5}$

Multiply $2\sqrt{3} \times \sqrt{6}$. Answer as a mixed radical.

 $2\sqrt{3} \times \sqrt{6}$

 $2 \times \sqrt{3} \times \sqrt{3 \times 2}$

We can multiply radicands.

 $=2\sqrt{(3\times3)\times2}$

Now simplify the new radical.

 $= 2 \times 3 \times \sqrt{2}$

 $= 2 \times 3 \times \sqrt{2}$

Write as a mixed radical.

 $= 6\sqrt{2}$

Multiply. Answer as a mixed radical.

 $(-3\sqrt{6})(5\sqrt{8})$

 $= (-3 \times 5 \times \sqrt{6} \times \sqrt{8})$

Multiply non-radicals, multiply radicands

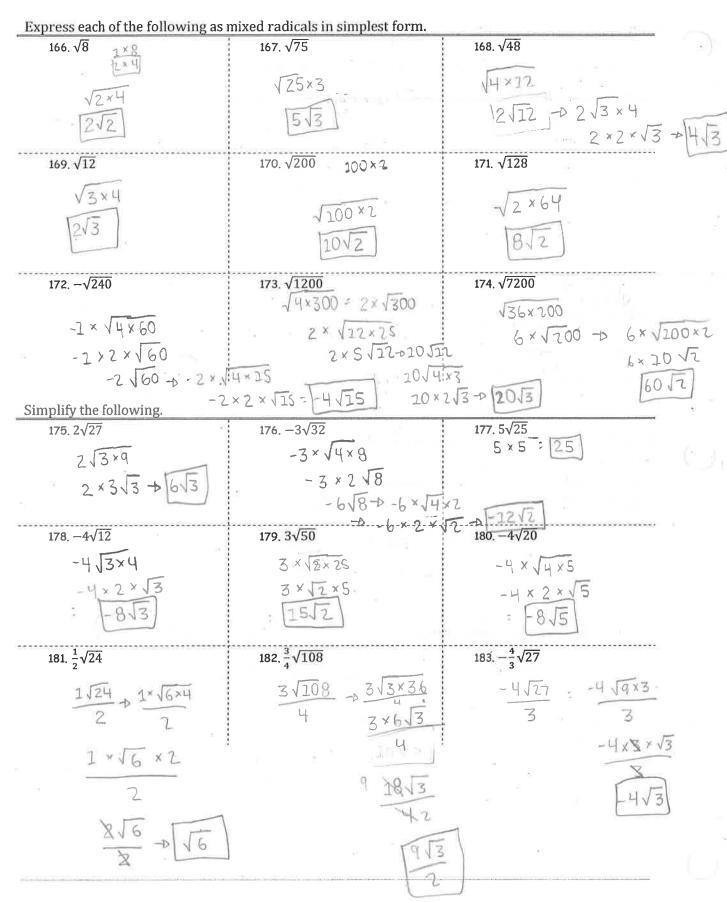
 $= (-3 \times 5 \times \sqrt{2 \times 3} \times \sqrt{2 \times 2 \times 2})$

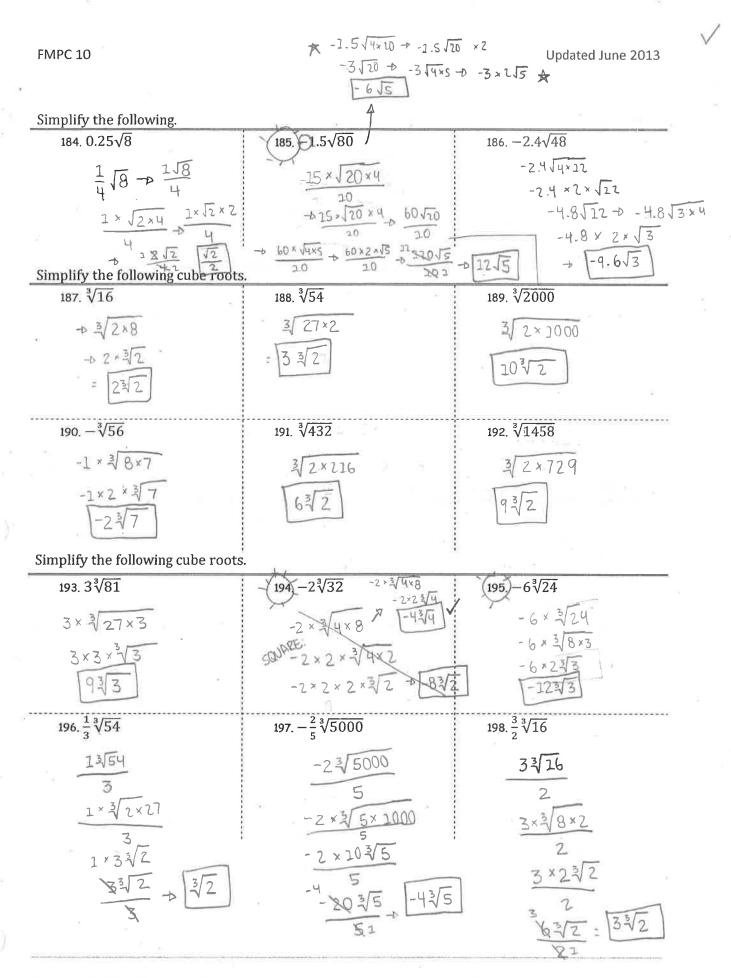
 $=-15 \times \sqrt{(2 \times 2) \times (2 \times 2) \times 3}$

 $=-15\times2\times2\times\sqrt{3}$

Notice there are two pairs of like factors

 $=-60\sqrt{3}$





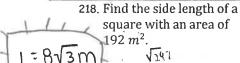
Answer the following. Simplify 199. Find the value of 'a'.	200. Find the va		201. Find the value of 'a'.	
_ [*				y +
$\sqrt{150} = a\sqrt{6}$		$=2a\sqrt{2}$	$\sqrt{96} = 4\sqrt{2a}$	
V-25 × 6 = a V 6		2:2aV2	V4x24= 452a	
5/6:0/6	81	Z: 2aV2	2/24 = 4 JZa	2025
[0:5]		q=4	2√6×4 : 4√2a	
202. The two shorter sides of a right tr cm. Using the Pythagorean Theor	riangle are 8 cm and 2 rem $a^2 + b^2 = c^2$, find	Using the Pyt	of an isosceles right triangle are 5 cm. hagorean Theorem $a^2 + b^2 = c^2$, find the	ne 5 46
the length of the third side in sim	plest radical form.	length of the	third side in simplest radical form. $\sqrt{2} \times 25$	V2 a
	V68	e .	V50 02+6	02: C2
8. 2	7			2 : C2
02+p2 = C2				25 = C2
82+22: 62				50:03
64+4 : C2	**		5 cm	√50: √
168:C - 14	x1 -0 2 \(\frac{1}{2}\) = C	*	* A	√50 ÷
[168.0]	* *	24	(5/2 LE	1×15 : C
204. Explain, using an example, how you using the multiplication of radical	ou simplify a radical ls method.	205 Explain, using using pairs of	g an example, how you simplify a radical prime factors of the radicand method.	5/2
		4 女		A
You can simplify a	radicăt	YOHLON!	t simplify Us	ina
y using the mult	Inlication	pairs of	prime fartor	< ?
of radicale wathing	4 hi	PALLS	PALLUX LWW.LYL	
Strate on 111th above a	. U \	Vall 64 15 1	im plify by findin	a
rusi munipying	100/00/2	You can s		J
so you get one ro	30/C0/	the prime	e factors and it th	ere ar e
and then you ca	n-	2 of the	same numbers yo	00
simplify that new	N O n e	KNOW that	f you can put the	at
radical, which wa	Sthe	outside.	the radical sign	
product of the c	mortainai	EXAMPLE:	150 → 1(5×5×2 = 15	V2
radicals	7			
EXAMPLE: 215 × 31	Ī0		entron and 1975 - 1953 (2006). Historicological is a communitation of a sillinoissii.	
= 2×3×√5	5 × \10	. <	-9-	
= 6√50	-'>		TEXT - E	
= 6V2×7	5		4 0	
= 6 × 5 √	2			\
Page 28 Real Numbers Key	2)		th permission. Do not use after June 20:	4.5

30 1/2 is a simplified radical of 21/3 × 3/10.

Multiply and simplify if possible,

$206.\sqrt{18}\times\sqrt{12}$	$207.3\sqrt{20}\times2\sqrt{5}$	$2085\sqrt{10} \times -2\sqrt{21}$
(3√2)(2√3)	6 × √100	10/210
6 16	[60]	
	2 =	
a		- An - *
$209.2\sqrt{7} \times 3\sqrt{1} \times \sqrt{7}$	210. $-2(3\sqrt{6})(-\sqrt{8})$	$211. \ 3\sqrt{7} \times 2\sqrt{6} \times -5\sqrt{2}$
6×149	-2×3×√6×-1×√8	-30/84
6×7= 42	6 × V 4.8	-30 V4×21
	6 \ 4 × 12	-30×2×√2
, ° , , , , , , , , , , , , , , , , , ,	6 ×2√3×4	1-60/2
	6×2×2√3	
'ast	24 1/3	
212. $-2(3\sqrt{2})^3$	213. $(3\sqrt{5})^3(2\sqrt{2})^3$	214. ($\sqrt[3]{9}$)($\sqrt[3]{9}$)
-Z×(3√2)×(3√2)×	(8√2)	3/9 × 3/9
54×18	3*15×3×15×3×15×2×12×2×12×2×12	3/81
-54 V2×4	216 \ 1000	3/3×27
- 54 × 2√2	216√200×10	
-108/2	226×10√10 2260√10	3 3/3
215. $\sqrt[3]{4} \times \sqrt[3]{8}$	216. $2\sqrt[3]{3} \times 5\sqrt[3]{18}$	217. $-\sqrt[3]{4} \times -3\sqrt[3]{12}$
215. V4 × V6	1.00	
	2×√√3×5×√√18	-1 × 3 4 × -3 × 3 5
₹4 × ₹8		-1 × 3/4 × -3 × 3/5
₹4 × ₹8	2×¾3×5×¾18	3 × 3 √48
3√4×3√8 3√32 3√4×8	$2 \times \sqrt[3]{3} \times 5 \times \sqrt[3]{18}$ $10 \times \sqrt[3]{54}$ $10 \times \sqrt[3]{2} \times 27$	3 × 3√6×8
₹4 × ₹8	2 × ¾3 × 5 × ¾18 10 × ¾54	3 × 3 √48

Simplify.



V297 192 m2 / 192 219. Find the side length of a square with an area of $250 cm^{2}$.

220. Find the area of a square with side lengths $2\sqrt{3}$ cm.

$$2\sqrt{3} \times 2\sqrt{3}$$

$$4 \times \sqrt{9}$$

$$4 \times 3 \rightarrow 12 \text{cm}^2$$

VI97 -> VUXU8 2 V9x17 -> 2×2 127 4 122 > 4 13 44 -> 41

221. Find the area of a rectangle in simplest radical form if the dimensions are $\sqrt{12}$ cm and $\sqrt{20}$ cm.

> 172 × 120 -> 1240 -> 14 × 60 D 2√60 → 2√4×15 2×2√15

222. Find the area of a rectangle in simplest radical form if the dimensions are $\sqrt{108}$ mm and $\sqrt{175}$ mm.

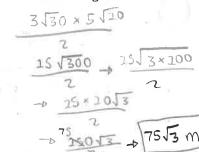
$$\sqrt{108} \times \sqrt{17} S = \sqrt{18900}$$
 $\sqrt{189} \times \sqrt{100} \rightarrow 10\sqrt{189} \rightarrow 10\sqrt{21} \times \sqrt{100}$
 $10 \times 3\sqrt{21} \rightarrow 30\sqrt{21} \text{ mm}^2$

223 Calculate the exact area (radical) of a triangle that has base $\sqrt{14}$ mm and a height $\sqrt{28}$ mm.

128 \ \ \frac{\sqr}{2} \ \frac{\sqr}{2} \ \frac{\sqr}{2} - 7 ×212 2 152 - 752 mm2

224. Calculate the exact area (radical) of a triangle that has base $5\sqrt{10}$ m and a height $3\sqrt{30}$ m.

3530



225 Find the length of a rectangle if its area is $6\sqrt{18}$ and its width is $3\sqrt{6}$

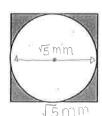
226. A rectangle has an area of $6\sqrt{15}$. Find possible side lengths that are mixed radicals.

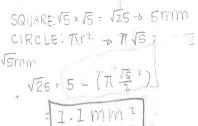
Factors of 6:

Factors of 15% 1×15, 3×5

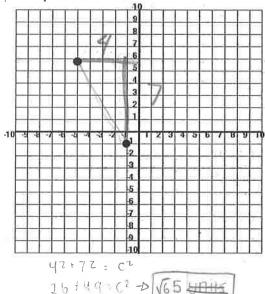
SIDE LENGTHS #1 = 213 × 315 SIDE LENGTHS # 2 = 215 × 313

227/A circle of diameter √5 mm is inscribed in a square. Find the area of the square not covered by the circle. Answer to the nearest tenth.

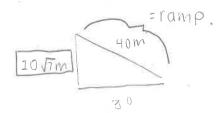




229. Find the distance between the two points in simplest radical form.

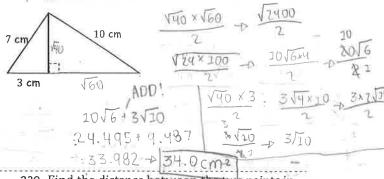


(231) A 40 m ramp extends from a floating dock up to a parking lot, a horizontal distance of 30 m. How high is the parking lot above the dock? Answer in simplest radical form.

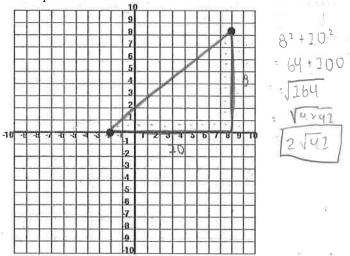


$$40^{2}-30^{2}=700$$
 $\sqrt{700}=\sqrt{7},100$
 $10\sqrt{7}$ m

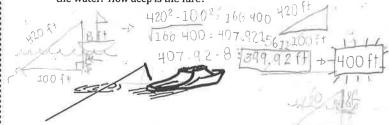
228 Find the area of the triangle below. Answer to the nearest tenth.



230. Find the distance between the two points in simplest radical form.



A fishing boat trolling in Haro Strait lets out 420 ft of fishing line. The lure at the end of the line is 100 ft behind the boat and the line starts 8 feet above the water. How deep is the lure?



What assumptions did you need to make to answer this question?

- 2). The pole was straight up.
- (2) the line is perfectly straight.
- 3 fishing pole is on edge of boar.

Writing Mixed Radicals as Entire Radicals.

Remember the process you used to simplify entire radicals → mixed radicals.

$$\sqrt{18} = \sqrt{9 \times 2} = 3\sqrt{2}$$

You will need to reverse the process...

Eg. Write $2\sqrt{5}$ as an entire radical.

$$2 \times \sqrt{5}$$

Convert the whole number, 2, to a radical. 2 is equivalent to $\sqrt{4}$

$$\sqrt{4} \times \sqrt{5}$$

Multiply the radicands.

$$=\sqrt{20}$$

Eg. Write $5\sqrt{6}$ as an entire radical.

$$5 \times \sqrt{6}$$

$$\sqrt{25} \times \sqrt{6}$$

Convert the whole number, 5, to a radical. 5 is equivalent to $\sqrt{25}$

$$=\sqrt{150}$$

Eg. Arrange in ascending order. $6\sqrt{2}$, $3\sqrt{7}$, $2\sqrt{17}$, $4\sqrt{5}$

$$6\sqrt{2} = \sqrt{36} \times \sqrt{2} = \sqrt{72}$$

$$3\sqrt{7} = \sqrt{9} \times \sqrt{7} = \sqrt{63}$$

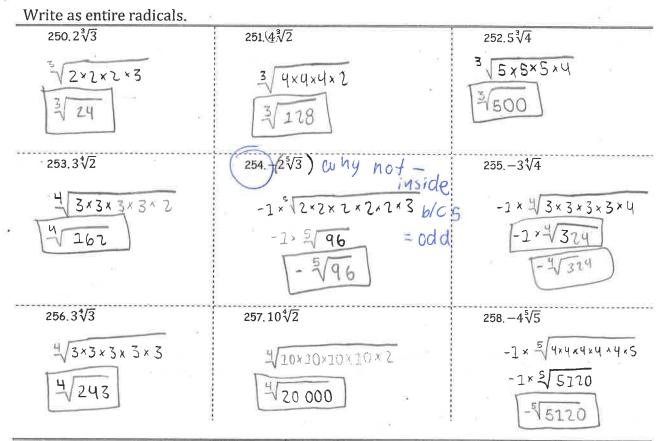
$$2\sqrt{17} = \sqrt{4} \times \sqrt{17} = \sqrt{68}$$

$$4\sqrt{5} = \sqrt{16} \times \sqrt{5} = \sqrt{80}$$

Ascending Order: $3\sqrt{7}$, $2\sqrt{17}$, $6\sqrt{2}$, $4\sqrt{5}$

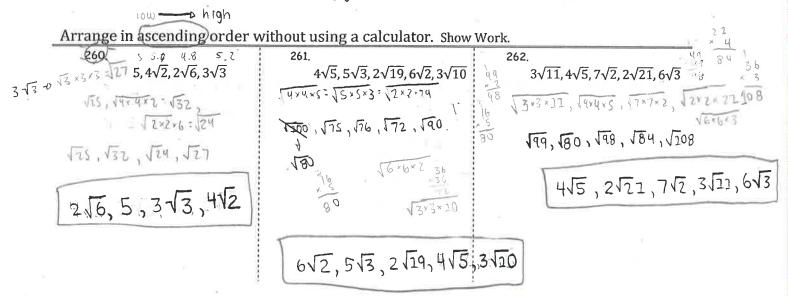
Write as entire radicals.

244.4√3	245.5√3	246.3√10
VI6 × V3 = [V48] -	√25×√3 = √75	$\sqrt{9} \times \sqrt{10} = \sqrt{90}$
2 4×4×3 = = 148		
247.10√3	248,04√5 seperate	249. —7√2
$\sqrt{100 \times \sqrt{3}}$ $\sqrt{10 \times 10 \times 3} = \sqrt{300}$	-1×\126 × \15 -1×\80	-1 × √49 × √2 -1 × √98 [-√98]



259. Explain, in detail, how you could arrange a list of irrational numbers written in simplified radical form in ascending order without using a calculator.

YOU don't need to use a calculator, you can change the simplified radicals into entire radicals and the radicands that are the biggest will be the biggest, etc.



Mixed Practice

263. What sets of numbers does $2\sqrt{5}$ belong? 215 \$ 12×2×5 = 120

Real (R), Irrational (Q)

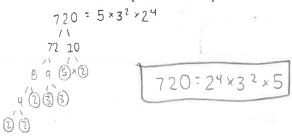
264. What sets of numbers does $\frac{12}{3}$ belong?

Real (R), Rational (Q), Integer (Z), whole (W), Natural (M)

265. Write the number 9 in the following forms:

- a) product of its primes 3×3
- b) as a radical

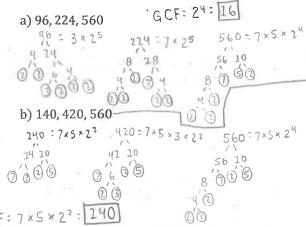
266. Write 720 as a product of its primes.



267. Explain how you could use the prime factors of 784 to find the square root. Then find the square root of 784.

- Find prime factors
- Use factors and divide into EQUAL parts (a product 2 EQUAL #S)

Multiply those (in one section to get square 268. Find the greatest common factor of the following sets of numbers.



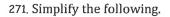
269. Write 512 as a product of its primes. Use the factors to find $\sqrt[3]{512}$.

3 V512 = 3 V(23) x (23) x (23) 3 V5I2 = (23) → 8

270. Use the pattern in the previous question to find $\sqrt[3]{a^9}$

$$3\sqrt{\alpha}9 = \sqrt[3]{(\alpha^3) \times (\alpha^3) \times (\alpha^2)}$$

$$\sqrt[3]{\alpha}9 = (\alpha^3)$$



a)
$$\sqrt{5} \times \sqrt{3} \Rightarrow \sqrt{15}$$

b)
$$-2\sqrt{7} \times 3\sqrt{5}$$

273. Multiply and simplify the following. $\sqrt{12} \times 2\sqrt{3}$

275. The "living space" in Kai's tree fort is a perfect cube. The volume of the living space is 104 m³. Find the area of carpet he will need to cover the floor. Answer to the nearest tenth.

AREA OF CARPET= 22.1m2

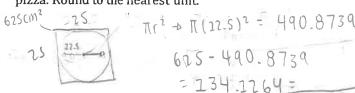
277. Find the perimeter of a square that has an area of 20 m². Answer as a mixed radical.

272. Simplify the following.

b)
$$-2\sqrt{180} = -2\sqrt{9\times20} - 2\times3\sqrt{4\times5} - 2\times3\times2\sqrt{5}$$

274. Multiply and simplify the following. $\sqrt{20} \times 2\sqrt{12}$

276. A pizza just fits inside of a square box with an area of 625 cm². Find the area of the bottom of the box that is not covered by the pizza. Round to the nearest unit.



278. Without a calculator, arrange the following in descending order.

in descending order. Show Work. $4\sqrt{5}$, $3\sqrt{6}$, $2\sqrt{10}$, $5\sqrt{3}$, $6\sqrt{2}$ $\sqrt{4\times4\times5}$, $\sqrt{3\times3\times6}$, $\sqrt{1\times2\times20}$, $\sqrt{5\times5\times7}$, $\sqrt{6\times6\times2}$ $\sqrt{80}$, $\sqrt{5}$ 4, $\sqrt{40}$, $\sqrt{7}$ 5, $\sqrt{7}$ 2

ADDITIONAL MATERIAL

Absolute Value: |x|

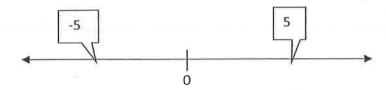
The Absolute Value of a real number is its numerical value ignoring its sign. Straight brackets around an expression indicate the absolute value function.

Eg. |5| reads "the absolute value of five."

Eg. |7 - 12| reads "the absolute value of seven minus twelve."

Absolute value is defined as the distance from zero on the number line.

Recall, distance cannot be a negative number. Both 5 and -5 are five units from zero.



Simplify the following.

1.
$$|-12| = 12$$

3.
$$||-2.54| = 2.54$$

The absolute value symbol is a type of bracket. This means that operations inside the symbol must be performed first.

Eg.
$$|2-5| = |-3| = 3$$

Eg.
$$-2|7-12| = -2|-5| = -2(5) = -10$$

Evaluate the following.

4.
$$|3+4-9|$$
 $|7-9| = |-2| = |2|$
5. $|\frac{-7}{2} + \frac{2}{3}| = |\frac{-21}{6} + \frac{4}{6}|$
6. $-|3(2-5)|$
 $-|3(-3)| = -|-9| = -|9|$
7. $-5|3+7|$
8. $|2-7|-|5+3|$
 $|-5|-|8|$
 $|5|-|8|$
 $|5|-|8|$
 $|5|-|8|$
 $|5|-|3|1|$
 $|5|-|3|1|$